

# Interactive Visual Analysis of Multi-Dimensional Scientific Data

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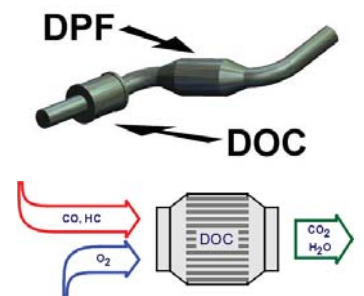
## Scientific data – one common view



- **Measured or simulated** data of some phenomenon
- Usually in relation to **space** and/or **time**
- Useful data model  $\mathbf{d}(\mathbf{x})$  with
  - domain  $\mathbf{x}$  (usually 2D or 3D space, time), independent variables
  - range  $\mathbf{d}$  (measured/simulated values), dependent values (dependent on  $\mathbf{x}$ )
- Typical examples:
  - CT data  $d(\mathbf{x})$  with  $\mathbf{x} \in \mathbb{R}^3$  and  $d \in \mathbb{R}$
  - unsteady 2D flow  $\mathbf{v}(\mathbf{x}, t)$  with  $\mathbf{x} \in \mathbb{R}^2$ ,  $t \in \mathbb{R}$ , and  $\mathbf{v} \in \mathbb{R}^2$
  - flow sim. result  $\mathbf{d}(\mathbf{x}, t)$  with  $\mathbf{x} \in \mathbb{R}^3$ ,  $t \in \mathbb{R}$ , and  $\mathbf{d} \in \mathbb{R}^n$
- Dimensionality?

# High-dimensional vs. multi-variate data

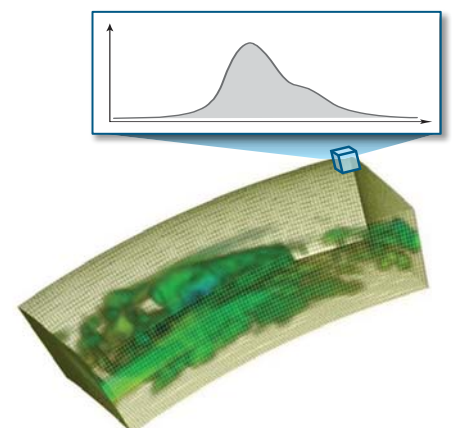
- **Increased dimensionality of  $\mathbf{d}(\mathbf{x})$  wrt.**
  - range  $\mathbf{d} \rightarrow$  multi-variate data
  - domain  $\mathbf{x} \rightarrow$  multi-dimensional data
- Very often in SciVis: neither  $\mathbf{d}$  nor  $\mathbf{x}$  is high-dim.!  
Examples: CT scan, vector field, etc.
- Also addressed: **multi-variate scientific data**
  - multi-variate simulation data
    - ex.: simulated Diesel particulate filter,  $\mathbf{x} \in \mathbb{R}^{3 \times R}$ ,  $\mathbf{d} \in \mathbb{R}^{37}$ : range 37-dim. (or so)
    - integrated visualization, IVA w/ L&B, dim.-reduction techniques, etc.
  - multi-modal measurements, ...



- Multi-dimensional scientific data?

# Multi-dimensional scientific data

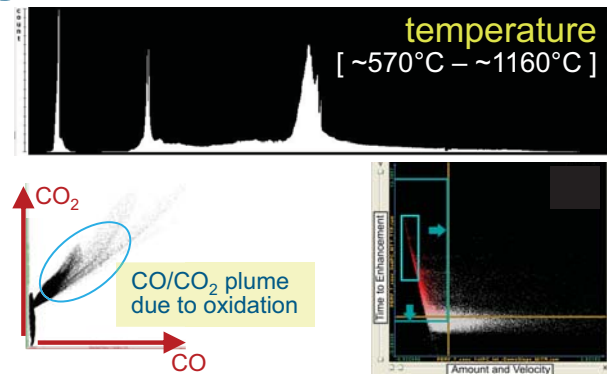
- More independent dimensions (more than space & time)
- One interesting & challenging class: **multi-run / ensemble data**
  - set of datasets, f.i.,
    - perturbed physics ensemble
    - initial condition ensemble
  - data  $\mathbf{d}(\mathbf{s}, t, \mathbf{p})$  w/  $\mathbf{d} \in \mathbb{R}^n$  – can be multi-variate, too – dependent on
    - space  $\mathbf{s}$  (2D or 3D)
    - time  $t$  (or not)
    - parameter(s)  $\mathbf{p}$ ,  $\mathbf{p} \in \mathbb{R}^m$
  - dealt with in
    - climatology
    - engineering
    - ...



# Interactive visual analysis

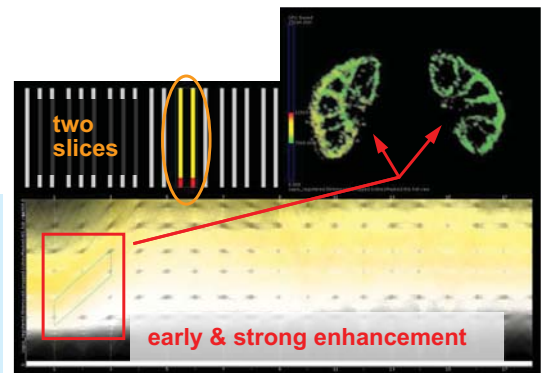
## Understanding data wrt. range $d$

- which distribution has data attribute  $d_i$ ?
- how do  $d_i$  and  $d_j$  relate to each other?
- which  $d_k$  discriminate data features?



## Understanding data wrt. domain $x$ ( $s$ , $t$ , and $p$ )

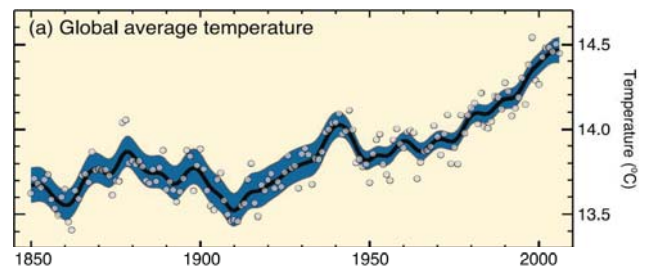
- where (in  $s$ ) are interesting data features?
- when (in  $t$ ) do they happen?
- how are they related to parameters  $p$ ?



# Investigating multi-run / ensemble data

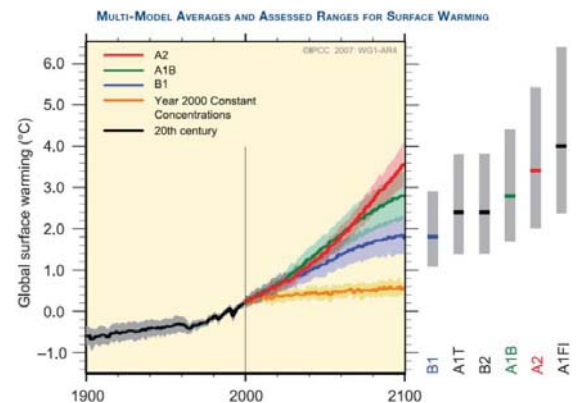
## Often: visualizing statistics

- trend (e.g., mean) & variation (std. dev.)
- data quartiles (e.g., via boxplots)

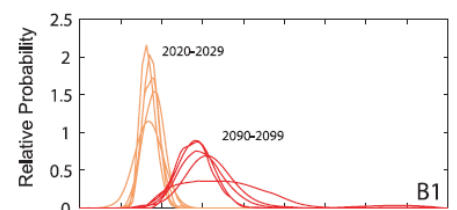


## Also: comparing aggregates

- statistics per run (class of runs)
- overlay of aggregates per run



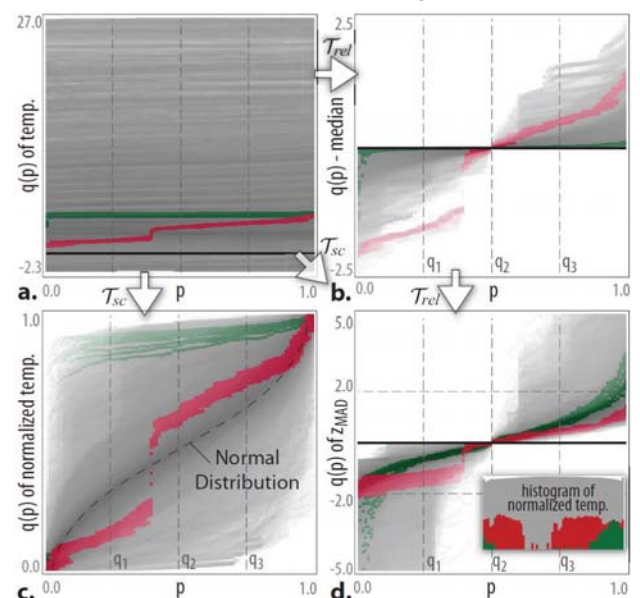
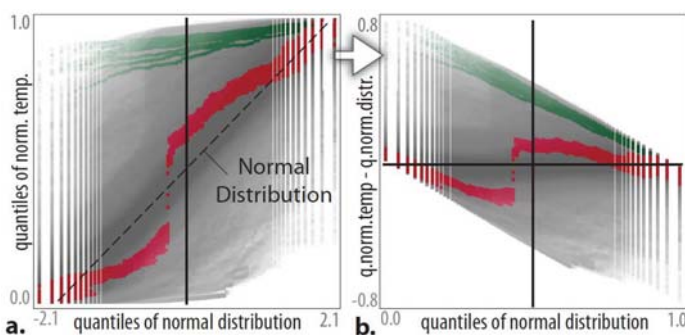
## One goal: sensitivity analysis



- Statistical aggregates across  $p$  to analyze
  - trends
    - mean  $\mu$ , std.-dev.  $\sigma$ , ...
    - quartiles  $q_1$ ,  $q_2$  (median), and  $q_3$ , IQR  $q_3 - q_1$ , ...
    - octiles  $e_i = q(i/8)$ , quantiles  $q(p)$  with  $p \in [0, 1]$
    - ...
  - outliers
    - mild outliers:  $< q_1 - 1.5 \cdot \text{IQR}$ ,  $> q_3 + 1.5 \cdot \text{IQR}$
    - strong outliers:  $< q_1 - 3 \cdot \text{IQR}$ ,  $> q_3 + 3 \cdot \text{IQR}$
    - data outside  $[-2, 2]$  after z-standardization:  $z = (x_i - \mu) / \sigma$
    - ...
  
- Computing **multi-variate** (statistics) data (per  $\mathbf{s} \times t$ ) from **multi-dimensional** (raw) data

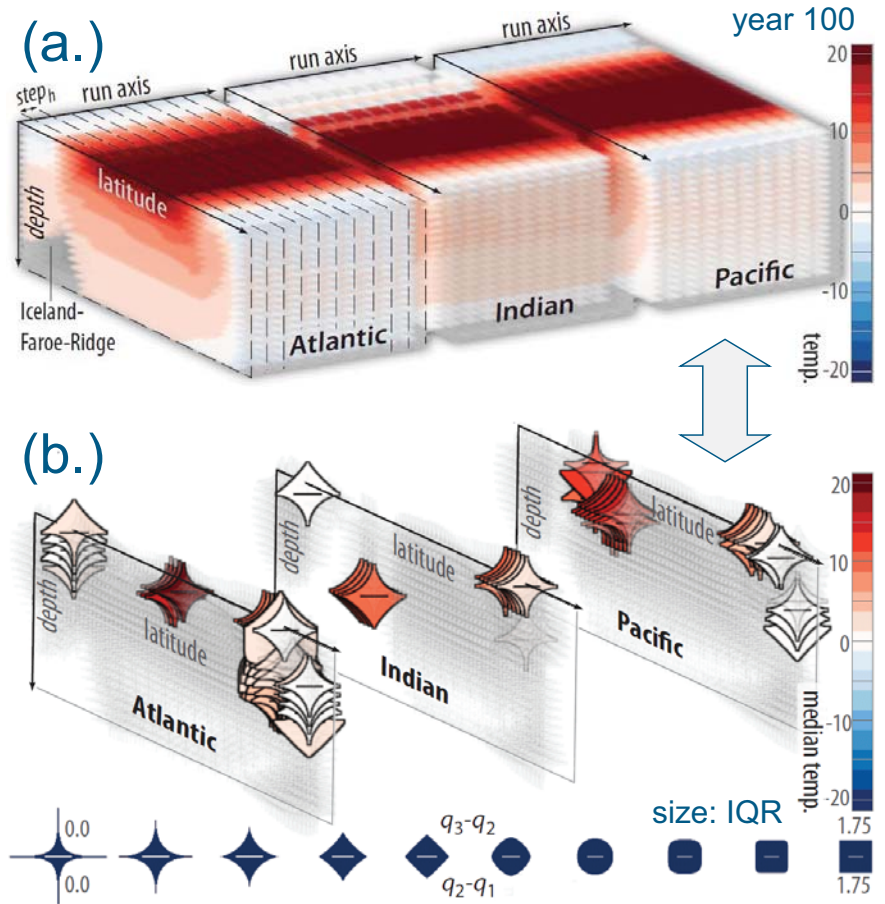
## Visualizing / analyzing lots of statistics

- Through statistical aggregation:
  - multiple statistics per spatiotemporal location
  - from  $d(\mathbf{s}, t, p)$  to  $\mu(\mathbf{s}, t)$ ,  $\sigma(\mathbf{s}, t)$ , etc.
- Useful views allow the interactive visual analysis
  - **quantile-plot**  $q(p)$  vs.  $p$ , here for numerous  $(\mathbf{s}, t)$
  - **detrending** (e.g.,  $-q_2$ ), **normalization** (e.g.,  $z$ )



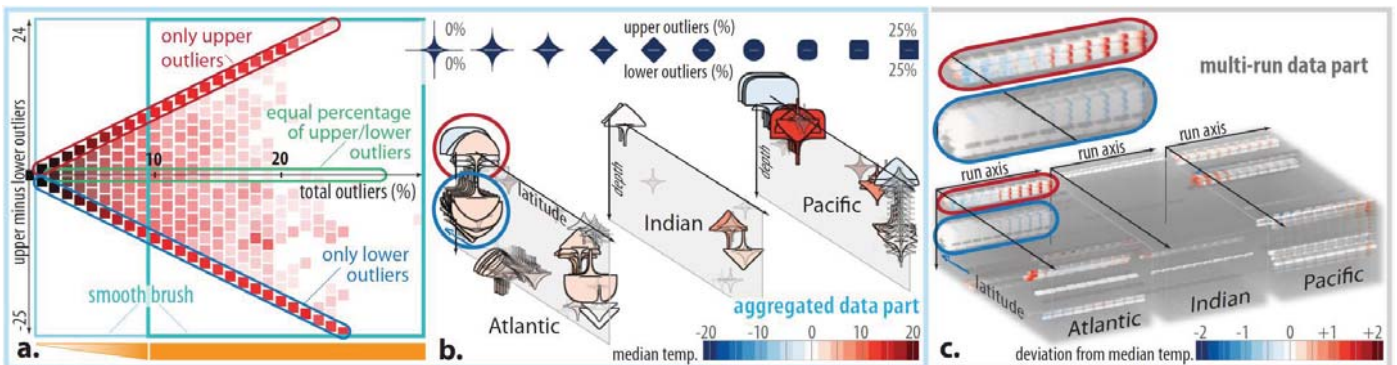
# Linking ensemble data and aggregates

- Climate sim. data (temp.)
  - Independent dimensions:
    - 3\* 2D slices (lat. × depth)
    - 500 years
    - 2 params. (10×10)
- a. All runs along 3<sup>rd</sup> dimension
- b. Glyphs show temp.-stats.



# Relating aggregates and raw data

- a. %outliers vs. upper–lower outliers (≥10%outliers brushed)
- b. linked glyphs locate brushed locations







- c. linked raw data vis shows responsible outlier runs

## Discussion, conclusions, questions

- **Multi-field** can be **multi-variate** or **multi-dimensional**
- **Multi-dimensional** scientific data **challenging**, **integrated statistical aggregation** can help
- **Visualization** on at least **two** (linked) **levels**
  - **aggregates** (transforming dims. into variates)
  - **original** (multi-dim.) **data**
- IVA reveals **trends**, but also **outliers**, helps to understand **distributions**
- Understanding **data features** **from statistical aggregates** is **challenging**
- Up to now according to an **Eulerian perspective** – Lagrangian, feature-based perspective?
- Other forms of multi-dimensional scientific data?

## Acknowledgements

- **Johannes Kehrer** () , **Peter Filzmoser** () , et al.
- **PIK** (Potsdam), **SimVis** (Vienna)  
- **You!** :-)

- **Brushing Moments in Interactive Visual Analysis** by J. Kehrer et al.; CGF 29(3):813–822, 2010
- **Interactive Visual Analysis of Heterogeneous Scientific Data across an Interface** by J. Kehrer et al.; TVCG 17(7):934–946, 2011